Andhra Pradesh State Council of Higher Education w.e.f. 2015-16 (Revised in April, 2016) B.A./B.Sc. FIRST YEAR MATHEMATICS SYLLABUS

SEMESTER -I, PAPER - 1 DIFFERENTIAL EQUATIONS

60 Hrs

UNIT - I (12 Hours), Differential Equations of first order and first degree:

Linear Differential Equations; Differential Equations Reducible to Linear Form; Exact Differential Equations; Integrating Factors; Change of Variables.

UNIT - II (12 Hours), Orthogonal Trajectories.

Differential Equations of first order but not of the first degree :

Equations solvable for p; Equations solvable for y; Equations solvable for x; Equations that do not contain. x (or y); Equations of the first degree in x and y – Clairaut's Equation.

UNIT – III (12 Hours), Higher order linear differential equations-I:

Solution of homogeneous linear differential equations of order n with constant coefficients; Solution of the non-homogeneous linear differential equations with constant coefficients by means of polynomial operators.

General Solution of f(D)y=0

General Solution of f(D)y=Q when Q is a function of x.

 $\frac{1}{f(D)}$ is Expressed as partial fractions.

P.I. of f(D)y = Q when $Q = be^{ax}$

P.I. of f(D)y = Q when Q is b sin ax or b cos ax.

UNIT - IV (12 Hours), Higher order linear differential equations-II:

Solution of the non-homogeneous linear differential equations with constant coefficients.

P.I. of f(D)y = Q when $Q = bx^k$

P.I. of f(D)y = Q when $Q = e^{ax}V$

P.I. of f(D)y = Q when Q = xV

P.I. of f(D)y = Q when $Q = x^m V$

UNIT -V (12 Hours), Higher order linear differential equations-HI:

Method of variation of parameters; Linear differential Equations with non-constant coefficients; The Cauchy-Euler Equation.

Reference Books:

- Differential Equations and Their Applications by Zafar Ahsan, published by Prentice-Hall of India Learning Pvt. Ltd. New Delhi-Second edition.
- A text book of mathematics for BA/BSc Vol 1 by N. Krishna Murthy & others, published by S. Chand & Company, New Delhi.
- Ordinary and Partial Differential Equations Raisinghania, published by S. Chand & Company, New Delhi.
- Differential Equations with applications and programs S. Balachandra Rao & HR . nuradhauniversities press.

Suggested Activities:

Seminar/ Quiz/ Assignments/ Project on Application of Differential Equations in Real life



B.A./B.Sc. FIRST YEAR MATHEMATICS SYLLABUS SEMESTER – II, PAPER - 2 SOLID GEOMETRY

60 Hrs

UNIT - I (12 hrs): The Plane:

Equation of plane in terms of its intercepts on the axis, Equations of the plane through the given points, Length of the perpendicular from a given point to a given plane, Bisectors of angles between two planes, Combined equation of two planes, Orthogonal projection on a plane.

UNIT - II (12 hrs): The Line:

Equation of a line; Angle between a line and a plane; The condition that a given line may lie in a given plane; The condition that two given lines are coplanar; Number of arbitrary constants in the equations of straight line; Sets of conditions which determine a line; The shortest distance between two lines; The length and equations of the line of shortest distance between two straight lines; Length of the perpendicular from a given point to a given line;

UNIT - III (12 hrs) : Sphere :

Definition and equation of the sphere; Equation of the sphere through four given points; Plane sections of a sphere; Intersection of two spheres; Equation of a circle; Sphere through a given circle; Intersection of a sphere and a line; Power of a point; Tangent plane; Plane of contact; Polar plane; Pole of a Plane; Conjugate points; Conjugate planes;

UNIT - IV (12 hrs) : Sphere & Cones :

Angle of intersection of two spheres; Conditions for two spheres to be orthogonal; Radical plane; Coaxial system of spheres; Simplified from of the equation of two spheres.

Definitions of a cone; vertex; guiding curve; generators; Equation of the cone with a given vertex and guiding curve; Enveloping cone of a sphere; Equations of cones with vertex at origin are homogenous; Condition that the general equation of the second degree should represent a cone; Condition that a cone may have three mutually perpendicular generators;

UNIT - V (12 hrs) Cones & Cylinders:

Intersection of a line and a quadric cone; Tangent lines and tangent plane at a point; Condition that a plane may touch a cone; Reciprocal cones; Intersection of two cones with a common vertex; Right circular cone; Equation of the right circular cone with a given vertex; axis and semi-vertical angle.

Definition of a cylinder; Equation to the cylinder whose generators intersect a given conic and are parallel to a given line; Enveloping cylinder of a sphere; The right circular cylinder; Equation of the right circular cylinder with a given axis and radius.

Reference Books:

- Analytical Solid Geometry by Shanti Narayan and P.K. Mittal, Published by S. Chand & Company Ltd. 7th Edition.
- A text book of Mathematics for BA/B.Sc Vol 1, by V Krishna Murthy & Others, Published by S. Chand & Company, New Delhi.
- A text Book of Analytical Geometry of Three Dimensions, by P.K. Jain and Khaleel Ahmed, Published by Wiley Eastern Ltd., 1999.
- 4. Co-ordinate Geometry of two and three dimensions by P. Balasubrahmanyam, K.Y. Subrahmanyam, G.R. Venkataraman published by Tata-MC Gran-Hill Publishers Company Ltd., New Delhi.

Suggested Activities:

Seminar/ Quiz/ Assignments/ Project on Application of Solid Geometry in Engineering



B.A./B.Sc. SECOND YEAR MATHEMATICS SYLLABUS SEMESTER - III, PAPER - 3

ABSTRACT ALGEBRA

60 Hrs

UNIT - 1: (10 Hrs) GROUPS: -

Binary Operation - Algebraic structure - semi group-monoid - Group definition and elementary properties Finite and Infinite groups - examples - order of a group. Composition tables with examples.

UNIT - 2: (14 Hrs) SUBGROUPS: -

Complex Definition - Multiplication of two complexes Inverse of a complex-Subgroup definition - examples-criterion for a complex to be a subgroups.

Criterion for the product of two subgroups to be a subgroup-union and Intersection of subgroups.

Co-sets and Lagrange's Theorem :-

Cosets Definition - properties of Cosets-Index of a subgroups of a finite groups-Lagrange's Theorem.

UNIT -3: (12 Hrs) NORMAL SUBGROUPS: -

Definition of normal subgroup - proper and improper normal subgroup-Hamilton group criterion for a subgroup to be a normal subgroup - intersection of two normal subgroups - Sub group of index 2 is a normal sub group - simple group - quotient group - criteria for the existence of a quotient group.

<u>UNIT - 4 : (10 Hrs) HOMOMORPHISM : -</u>

Definition of homomorphism - Image of homomorphism elementary properties of homomorphism - Isomorphism - aultomorphism definitions and elementary properties-kernel of a $homomorphism-fundamental\ theorem\ on\ Homomorphism\ and\ applications.$

<u>UNIT - 5 : (14 Hrs) PERMUTATIONS AND CYCLIC GROUPS : -</u>

Definition of permutation - permutation multiplication - Inverse of a permutation - cyclic permutations - transposition - even and odd permutations - Cayley's theorem.

Cyclic Groups :-

Definition of cyclic group - elementary properties - classification of cyclic groups.

Reference Books:

- 1. Abstract Algebra, by J.B. Fraleigh, Published by Narosa Publishing house.
- 2. A text book of Mathematics for B.A. / B.Sc. by B.V.S.S. SARMA and others, Published by S.Chand & Company, New Delhi.
- 3. Modern Algebra by M.L. Khanna.

Suggested Activities:

Seminar/ Quiz/ Assignments/ Project on Group theory and its applications in Graphics and Medical image Analysis



B.A./B.Sc. SECOND YEAR MATHEMATICS SYLLABUS

SEMESTER - IV, PAPER- 4 REAL ANALYSIS

60 Hrs

UNIT - I (12 hrs) : REAL NUMBERS :

The algebraic and order properties of R, Absolute value and Real line, Completeness property of R, Applications of supreme property; intervals. No. Question is to be set from this portion.

<u>Real Sequences:</u> Sequences and their limits, Range and Boundedness of Sequences, Limit of a sequence and Convergent sequence.

The Cauchy's criterion, properly divergent sequences, Monotone sequences, Necessary and Sufficient condition for Convergence of Monotone Sequence, Limit Point of Sequence, Subsequences and the Bolzano-weierstrass theorem — Cauchy Sequences — Cauchey's general principle of convergence theorem.

UNIT -II (12 hrs): INFINITIE SERIES:

<u>Series</u>: Introduction to series, convergence of series. Cauchey's general principle of convergence for series tests for convergence of series, Series of Non-Negative Terms.

- 1. P-test
- 2. Cauchey's nth root test or Root Test.
- 3. D'-Alemberts' Test or Ratio Test.
- 4. Alternating Series Leibnitz Test.

Absolute convergence and conditional convergence, semi convergence.

UNIT - III (12 hrs) : CONTINUITY :

Limits: Real valued Functions, Boundedness of a function, Limits of functions. Some extensions of the limit concept, Infinite Limits. Limits at infinity. No. Question is to be set from this portion.

Continuous functions: Continuous functions, Combinations of continuous functions, Continuous Functions on intervals, uniform continuity.

UNIT - IV (12 lirs): DIFFERENTIATION AND MEAN VALUE THEORMS:

The derivability of a function, on an interval, at a point, Derivability and continuity of a function, Graphical meaning of the Derivative, Mean value Theorems; Role's Theorem, Lagrange's Theorem, Cauchhy's Mean value Theorem

UNIT - V (12 hrs): RIEMANN INTEGRATION:

Riemann Integral, Riemann integral functions, Darboux theorem. Necessary and sufficient condition for R – integrability, Properties of integrable functions, Fundamental theorem of integral calculus, integral as the limit of a sum, Mean value Theorems.

Reference Books:

- 1. Real Analysis by Rabert & Bartely and .D.R. Sherbart, Published by John Wiley.
- A Text Book of B.Sc Mathematics by B.V.S.S. Sarma and others, Published by S. Chand & Company Pvt. Ltd., New Delhi.
- 3. Elements of Real Analysis as per UGC Syllabus by Shanthi Narayan and Dr. M.D. Raisingkania Published by S. Chand & Company Pvt. Ltd., New Delhi.

Suggested Activities:

Seminar/ Quiz/ Assignments/ Project on Real Analysis and its applications



B.A./B.Sc. THIRD YEAR MATHEMATICS SYLLABUS SEMESTER - V, PAPER -5 RING THEORY & VECTOR CALCULUS

UNIT - 1 (12 hrs) RINGS-I: -

60 Hrs

Definition of Ring and basic properties, Boolean Rings, divisors of zero and cancellation laws Rings, Integral Domains, Division Ring and Fields, The characteristic of a ring - The characteristic of an Integral Domain, The characteristic of a Field. Sub Rings, Ideals

UNIT - 2 (12 hrs) RINGS-II:

Definition of Homomorphism - Homorphic Image - Elementary Properties of Homomorphism -Kernel of a Homomorphism - Fundamental theorem of Homomorhphism -Maximal Ideals - Prime Ideals.

UNIT -3 (12 hrs) VECTOR DIFFERENTIATION: -

Vector Differentiation, Ordinary derivatives of vectors, Differentiability, Gradient, Divergence, Curl operators, Formulae Involving these operators.

UNIT - 4 (12 hrs) VECTOR INTEGRATION:-

Line Integral, Surface Integral, Volume integral with examples.

UNIT - 5 (12 hrs) VECTOR INTEGRATION APPLICATIONS :-

Theorems of Gauss and Stokes, Green's theorem in plane and applications of these theorems.

Reference Books :-

- 1. Abstract Algebra by J. Fralieh, Published by Narosa Publishing house.
- 2. Vector Calculus by Santhi Narayana, Published by S. Chand & Company Pvt. Ltd., New Delhi.
- 3. A text Book of B.Sc., Mathematics by B.V.S.S.Sarma and others, published by S. Chand & Company Pvt. Ltd., New Delhi.
- 4. Vector Calculus by R. Gupta, Published by Laxmi Publications.
- 5. Vector Calculus by P.C. Matthews, Published by Springer Verlag publicattions.
- 6. Rings and Linear Algebra by Pundir & Pundir, Published by Pragathi Prakashan.

Suggested Activities:

Seminar/ Quiz/ Assignments/ Project on Ring theory and its applications



B.A./B.Sc. THIRD YEAR MATHEMATICS SYLLABUS SEMESTER - V, PAPER -6 LINEAR ALGEBRA

60 Hrs

UNIT - I (12 hrs) : Vector Spaces-I:

Vector Spaces, General properties of vector spaces, n-dimensional Vectors, addition and scalar multiplication of Vectors, internal and external composition, Null space, Vector subspaces, Algebra of subspaces, Linear Sum of two subspaces, linear combination of Vectors, Linear span Linear independence and Linear dependence of Vectors.

UNIT -II (12 hrs) : Vector Spaces-II :

Basis of Vector space, Finite dimensional Vector spaces, basis extension, co-ordinates, Dimension of a Vector space, Dimension of a subspace, Quotient space and Dimension of Quotientspace.

UNIT -III (12 hrs): Linear Transformations:

Linear transformations, linear operators, Properties of L.T, sum and product of LTs, Algebra of Linear Operators, Range and null space of linear transformation, Rank and Nullity of linear transformations – Rank – Nullity Theorem.

UNIT -IV (12 hrs) : Matrix :

Matrices, Elementary Properties of Matrices, Inverse Matrices, Rank of Matrix, Linear Equations, Characteristic Roots, Characteristic Values & Vectors of square Matrix, Cayley – Hamilton Theorem.

UNIT -V (12 hrs) : Inner product space :

Inner product spaces, Euclidean and unitary spaces, Norm or length of a Vector, Schwartz inequality, Triangle in Inequality, Parallelogram law, Orthogonality, Orthonormal set, complete orthonormal set, Gram – Schmidt orthogonalisation process. Bessel's inequality and Parseval's Identity.

Reference Books:

- 1. Linear Algebra by J.N. Sharma and A.R. Vasista, published by Krishna Prakashan Mandir, Meerut-250002.
- 2. Matrices by Shanti Narayana, published by S.Chand Publications.
- 3. Linear Algebra by Kenneth Hoffman and Ray Kunze, published by Pearson Education (low priced edition), New Delhi.
- Linear Algebra by Stephen H. Friedberg et al published by Prentice Hall of India Pvt. Ltd. 4th Edition 2007.

Suggested Activities:

Seminar/ Quiz/ Assignments/ Project on "Applications of Linear algebra Through Computer Sciences"



B.A./B.Sc. THIRD YEAR MATHEMATICS SYLLABUS SEMESTER – VI, PAPER – VII-(A) ELECTIVE-VII(A); LAPLACE TRANSFORMS

60 Hrs

UNIT - 1 (12 hrs) Laplace Transform I:-

Definition of - Integral Transform - Laplace Transform Linearity, Property, Piecewise continuous Functions, Existence of Laplace Transform, Functions of Exponential order, and of Class A.

UNIT - 2 (12 hrs) Laplace Transform II:-

First Shifting Theorem, Second Shifting Theorem, Change of Scale Property, Laplace Transform of the derivative of f(t), Initial Value theorem and Final Value theorem.

UNIT - 3 (12 hrs) Laplace Transform III : -

 $\label{eq:Laplace Transform of Integrals - Multiplication by t, Multiplication by t^n-Division by t. Laplace transform of Bessel Function, Laplace Transform of Error Function, Laplace Transform of Sine and cosine integrals.}$

UNIT -4 (12 hrs) Inverse Laplace Transform I:-

Definition of Inverse Laplace Transform. Linearity, Property, First Shifting Theorem, Second Shifting Theorem, Change of Scale property, use of partial fractions, Examples.

UNIT -5 (12 hrs) Inverse Laplace Transform II:-

Inverse Laplace transforms of Derivatives-Inverse Laplace Transforms of Integrals – Multiplication by Powers of 'P'- Division by powers of 'P'- Convolution Definition – Convolution Theorem – proof and Applications – Heaviside's Expansion theorem and its Applications.

Reference Books :-

- Laplace Transforms by A.R. Vasistha and Dr. R.K. Gupta Published by Krishna Prakashan Media
 Pvt. Ltd. Meerut.
- Fourier Series and Integral Transforms by Dr. S. Sreenadh Published by S.Chand and Co., Pvt. Ltd., New Delhi.
- Laplace and Fourier Transforms by Dr. J.K. Goyal and K.P. Gupta, Published by Pragathi Prakashan, Meerut.
- 4. Integral Transforms by M.D. Raising hania, H.C. Saxsena and H.K. Dass Published by S. Chand and Co., Pvt.Ltd., New Delhi.

Suggested Activities:

Seminar/ Quiz/ Assignments



B.A./B.Sc. THIRD YEAR MATHEMATICS SYLLABUS, SEMESTER - VI, CLUSTER - A, PAPER - VIII-A-1 Cluster Elective- VIII-A-1: INTEGRAL TRANSFORMS

60 Hrs

UNIT - 1 (12 hrs) Application of Laplace Transform to solutions of Differential Equations:

Solutions of ordinary Differential Equations.

Solutions of Differential Equations with constants co-efficient

Solutions of Differential Equations with Variable co-efficient

UNIT - 2 (12 kms) Application of Laplace Transform: -

Solution of simultaneous ordinary Differential Equations. Solutions of partial Differential Equations.

UNI) - 3 (12 hrs) Application of Laplace Transforms to Integral Equations : -

Definitions: Integral Equations-Abel's, Integral Equation-Integral Equation of Convolution Type, Integro Differential Equations. Application of L.T. to Integral Equations.

UNIT -4 (: 2 hrs) Fourier Transforms-I:-

Definition of Fourier Transform - Fourier's in Transform - Fourier cosine Transform - Linear Property of Fourier Transform - Change of Scale Property for Fourier Transform - sine Transform and cosine transform shifting property - modulation theorem.

UNIT - 5 (12 :---) Fourier Transform-II :-

Convolution Definition - Convolution Theorem for Fourier transform - parseval's Indentify -Relationship between Fourier and Laplace transforms - problems related to Integral Equations.

Finte Fourier Transforms : -

Finte Fourier Sine Transform - Finte Fourier Cosine Transform - Inversion formula for sine and cosine Transforms only statement and related problems.

Reference Books :-

- 1. Integral Transforms by A.R. Vasistha and Dr. R.K. Gupta Published by Krishna Prakashan Media Pvt. Ltd. Meerut.
- 2. A Course of Mathematical Analysis by Shanthi Narayana and P.K. Mittal, Published by S. Chand and Company pvt. Ltd., New Delhi.
- 3. Fourier Series and Integral Transforms by Dr. S. Sreenadh Published by S.Chand and Company Pvt. Ltd., New Delhi.
- 4. Lapalce and Fourier Transforms by Dr. J.K. Goyal and K.P. Gupta, Published by Pragathi Prakashan, Meerut.
- 5. Integral Transforms by M.D. Raising hania, H.C. Saxsena and H.K. Dass Published by S.Chand and Company pvt. Ltd., New Delhi.

Suggested Activities:

Seminar/ Quiz/ Assignments



B.A./B.Sc. THIRD YEAR MATHEMATICS SYLLABUS SEMESTER - VI: PAPER - VIII-A-2

ELECTIVE - VIII-A-2: ADVANCED NUMERICAL ANALYSIS

60 Hrs

Unit - I (10 Hours)

Curve Fitting: Least - Squares curve fitting procedures, fitting a straight line, nonlinear curve fitting, Curve fitting by a sum of exponentials.

UNIT- II: (12 hours)

Numerical Differentiation: Derivatives using Newton's forward difference formula, Newton's backward difference formula, Derivatives using central difference formula, stirling's interpolation formula, Newton's divided difference formula, Maximum and minimum values of a tabulated function.

UNIT- III: (12 hours)

Numerical Integration: General quadrature formula on errors, Trapozoidal rule, Simpson's 1/3 – rule, Simpson's 3/8 – rule, and Weddle's rules, Euler – Maclaurin Formula of summation and quadrature, The Euler transformation.

UNIT - IV: (14 hours)

Solutions of simultaneous Linear Systems of Equations: Solution of linear systems – Direct methods, Matrix inversion method, Gaussian elimination methods, Gauss-Jordan Method, Method of factorization, Solution of Tridiagonal Systems, Iterative methods. Jacobi's method, Gauss-siedal method.

UNIT - V (12 Hours)

Numerical solution of ordinary differential equations: Introduction, Solution by Taylor's Series, Picard's method of successive approximations, Euler's method, Modified Euler's method, Runge - Kutta methods.

Reference Books:

- 1. Numerical Analysis by S.S.Sastry, published by Prentice Hall India (Latest Edition).
- Numerical Analysis by G. Sankar Rao, published by New Age International Publishers, New Hyderabad.
- Finite Differences and Numerical Analysis by H.C Saxena published by S. Chand and Company, Pvt. Ltd., New Delhi.
- 4. Numerical methods for scientific and engineering computation by M.K.Jain, S.R.K.Iyengar, R.K. Jain.

Suggested Activities:

Seminar/ Quiz/ Assignments

